

# Understanding security failures of anonymous authentication schemes for cloud environments

Meijia Xu<sup>a,b</sup>, Ding Wang<sup>a,b,\*</sup>, Qingxuan Wang<sup>a,b</sup>, Qiaowen Jia<sup>c</sup>

<sup>a</sup> College of Cyber Science, Nankai University, Tianjin 300350, China

<sup>b</sup> Tianjin Key Laboratory of Network and Data Security Technology, Nankai University, Tianjin 300350, China

<sup>c</sup> Institute of Software, Chinese Academy of Sciences, Beijing 100190, China

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## ABSTRACT

Currently, password-based remote authentication mechanism has become an essential procedure to ensure users access the resources of the cloud server securely. Dozens of password-based multi-factor authentication schemes have been successively proposed recently. Unfortunately, most of them are vulnerable to various known attacks. The key to designing a secure and privacy-preserving authentication scheme is drawing some lessons from the security failures of existing schemes. In this work, we investigate three anonymous multi-factor authentication schemes based on passwords for cloud environments (i.e., Karuppiah et al.'s scheme at MONET'19, Lin's scheme at IEEE Syst J'19, Rajamanickam et al.'s scheme at IEEE Syst J'20), and demonstrate that these three schemes all suffer from off-line guessing attacks and are short of an important property (i.e., forward secrecy). We also propose several effective countermeasures to remedy these weaknesses. Our analysis shows that none of these three protocols can achieve their security goals. Furthermore, we make a summary of the causes of the flaws, and reveal that the vulnerabilities of these schemes are caused by violating the basic design principles for a secure protocol (e.g., Ma et al.'s principles at IJCS'14). In addition, we investigate whether dozens of recently proposed schemes follow the design principles of Ma et al.

## 1. Introduction

Nowadays, in the wake of the progress of information technology, various technologies related to the cloud are developing rapidly [1]. Cloud computing has been widely used in all walks of life because of its advantages such as broadband interconnection, shared resource pool, and flexible configuration. For enterprises, cloud computing can help reduce the maintenance costs of computing and storage. For individuals, deploying data storage and computing on cloud servers can eliminate constraints caused by limited storage resources. However, in cloud computing, due to user's data are stored in the remote cloud server, users will lose control of the data, which means that it cannot guarantee the security of the data [2,3]. Therefore, it is necessary to design the corresponding security mechanism for cloud computing to protect the confidentiality, integrity and availability of data on the cloud server. In order to achieve the above goal, Zhang et al. proposed a quantum-safe identity-based data outsourcing scheme with public integrity verification in cloud storage (DOPIV) [4]. However, sooner after that, Wang et al. [5] reveal that Zhang et al.'s mechanism is invalid because they only pay attention to the security of the data but

ignore the identity authentication, which is the first line of defense to ensure the security of information systems [6,7]. Therefore, the failure of Zhang et al. proved that the identity authentication is a necessary security mechanism to ensure the security of users' data. Meanwhile, since the cloud service has the characteristics of openness and resource sharing, we also need to protect the cloud server's service to prevent unauthorized users from abusing the resources of the server. There have been a number of attacks related to the security issues mentioned above, which allow attackers to impersonate legitimate users to steal users' data or misuse cloud servers' resources [8]. Solving the security issues of cloud computing is the top priority for the continued development of the cloud computing. Consequently, the identity authentication scheme is an indispensable part of cloud services. It is essential to ensure malicious attackers and unauthorized users cannot access the services of remote cloud servers in open environments [9].

### 1.1. Related works

As mentioned before, the cloud environment faces the threats of malicious attackers who can eavesdrop, interrupt, intercept and modify

\* Correspondence to: Ding Wang, College of Cyber Science, Nankai University, No. 38 Tongyan Road, Jinnan Distric, Tianjin 300350, China.

E-mail addresses: [xumeijia@mail.nankai.edu.cn](mailto:xumeijia@mail.nankai.edu.cn) (M. Xu), [wangding@nankai.edu.cn](mailto:wangding@nankai.edu.cn) (D. Wang), [wangqingxuan@mail.nankai.edu.cn](mailto:wangqingxuan@mail.nankai.edu.cn) (Q. Wang), [jiaqw@ios.ac.cn](mailto:jiaqw@ios.ac.cn) (Q. Jia).

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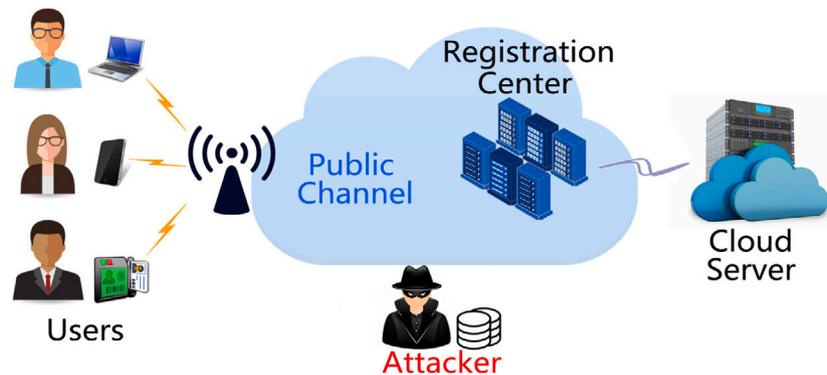


Fig. 1. Password-based authentication for the cloud services environment.

messages in the open channel, which accords to the standard Dolev-Yao model [10]. Accordingly, the designer is confronted with an impressive list of security goals (e.g., the resistance of impersonation attacks, replay attacks, and insider attacks). Most of the existing remote authentication schemes (e.g., [11,12]) for cloud environments are built on the basis of generic two-factor authentication schemes like [13,14].

In 1981, the authentication scheme based on passwords was first suggested by Lamport [15]. In this scheme, the user who owns the correct identity and password can pass the server's authentication. Since then, a series of password-based authentication protocols [16–21] sprang up. In 1991, Chang et al. [22] proposed the first smart-card-based two-factor password authentication scheme, which introduces a new authentication factor to improve the security of the authentication. However, these password-based schemes (e.g., [16,22]) are considered vulnerable after they were proposed. More specifically, they need to maintain a table to store the user's password or private parameters on the server side, which leads to stolen-verifier attacks or off-line dictionary attacks. In 1999, Yang et al. [23] proposed a new authentication scheme to overcome the above flaws. This scheme is the first two-factor scheme without a private parameters table on the server side. The security of these schemes are under the tamper-resistance assumption of the smart card.

Unfortunately, some research results have demonstrated that the security parameters stored in smart cards could be revealed or partially extracted by the state-of-the-art reverse engineering techniques [24] and side-channel attacks [25] (e.g., differential power analysis). To overcome this issue, in 2009, Xu et al. [26] proposed a two-factor authentication scheme based on smart card. They stated the scheme's security under the non-tamper resistance assumption. However, in 2010, Sood et al. [27] found that Xu et al.'s scheme cannot resist user impersonation attacks. After that, Song et al. [28] also found the weakness of Xu et al.'s scheme as mentioned before and proposed an improved scheme to fix the flaw in Xu et al.'s scheme [26]. In 2012, Chen et al. [29] revealed that both Sood et al.'s scheme [27] and Song et al.'s scheme [28] are still vulnerable. For nearly a decade, the history of the two-factor authentication has been a repeat of "break-fix-break-fix" [13]. Most scheme designers only pay attention to the modification and enhancement of a single protocol, but few designers consider the general design principles of a certain type of authentication schemes. In 2014, Ma et al. [30] proposed three vital design principles for the secure two-factor scheme based on smart cards, which has made a profound impact on the development of designing a secure scheme. Based on the design principles proposed by Ma et al. several designers have enhanced the security, efficiency, and anonymity of the two-factor authentication schemes (see Wang et al.' scheme at IEEE TDSC'18 [13], Li et al.'s scheme at IEEE TDSC' 20 [20]).

Most of the secure schemes mentioned above are suitable for single-server architecture of the cloud computing. This means that when the user log-in to different cloud servers, she needs to memorize corresponding different users identities and passwords [31] for different

cloud servers, which causes a burden for users. To reduce the burden of user's memory, in 2013, yang et al. [32] proposed a two-factor authentication scheme for multi-server cloud environments. After that, a series of schemes [31,33–38] were presented to solve the usability problem of authentication in the multi-server cloud environments recent years. As shown in Fig. 1, different from single-server schemes, in addition to users and cloud servers, the register center (also called the center server) is also a part of participants. Both the servers and the users need to register in the register center. Therefore, the user only needs to memorize one identity and corresponding password to access all the servers under the control of the register center [32]. Compared with single-server architecture schemes for cloud environments, these schemes for the multi-server architecture reduce the user's memory burden [31].

## 1.2. Motivation and contributions

In spite of authentication schemes for cloud environments have been developed for more than 10 years, it is still far from satisfactory. The history of the research area is a designer first proposes a scheme, then other researchers reveal this scheme is insecure to various attacks and propose several possible countermeasures to fix this scheme. The research rhythm is monotonous and some common problems are repeated. The whole field is struggling to move forward. Identifying the common problems and finding ways to solve them is of great importance to the development of the field.

Recently, Karupiah et al. [39] demonstrate that there are some security limitations in Kaul-Awasithi et al.'s scheme [40] proposed in 2016. Therefore, in 2019, Karupiah et al. [39] proposed an improved scheme to overcome Kaul-Awasithi et al.'s [40] flaws. They claim that the proposed scheme can resist the known attacks with lower computing and storage than other related schemes and the scheme performs better compared with other related schemes. In addition, Lin [37] and Rajamanickam et al. [38] proposed two different schemes for multi-server cloud environments. Lin [37] proposes a scheme simultaneously fulfilling preauthentication and postauthentication, which is a novel feature for the authentication scheme. Meanwhile, Lin proves his scheme's security under the random oracle model. Different from Lin [37], Rajamanickam et al. [38] pay more attention to insider attacks, which is a long-standing vulnerability for cloud environments. They proposed a novel authentication protocol for insider attacks based on a robust cryptographic algorithm, ECC. In addition to insider attacks, they claim that their scheme also can resist other known attacks.

In this work, we investigate three different schemes for cloud environments recently presented by Karupiah et al. [39], Lin [37] and Rajamanickam et al. [38]. Each of them claims to achieve their own ambitious design goals. Unfortunately, we reveal that none of them can achieve the security goals they claimed. We find all of them suffer from off-line guessing attack and cannot achieve forward secrecy. To

**Table 1**  
Capabilities of the adversary.

C-01	$\mathcal{A}$ can enumerate the space of $ D_{id}  \times  D_{pw} $ .
C-02	$\mathcal{A}$ can obtain the victim $U_i$ 's identity $ID_i$ .
C-1	$\mathcal{A}$ can full control of the public channel used for communication.
C-2	$\mathcal{A}$ can either (i) use malicious card readers to learn the user's password, or (ii) use side-channel attacks to extract the secret data in the card.
C-3	$\mathcal{A}$ can learn the previous session key(s) between the user and the server.
C-4	$\mathcal{A}$ can obtain the server's long-time private key(s) and other data stored in the server only when analyzing the forward secrecy or the root cause of the server's failure (e.g., known key attacks).

learn some lessons, we discuss the causes of the pitfalls and propose several possible countermeasures to overcome them. Last but not least, we analyze many different schemes proposed recently [37–47] and discuss the three basic principles of designing a secure scheme at Ma et al. [30]. We believe this work will spark interest for the designers to propose a password-based authentication scheme that achieved all essential security goals.

### 1.3. Organization

The rest of the paper is organized as follows: The capabilities of the adversary  $\mathcal{A}$  are introduced in Section 2. The cryptanalysis of the scheme of Karupiah et al. [39] is given in Section 3. And the cryptanalysis of the scheme of Lin [37] is given in Section 4. Section 5 gives the cryptanalysis of Rajamanickam et al.'s [38] scheme. The Section 6 discusses the causes of the pitfalls and Ma et al.'s three basic principles for protocol design. And Section 7 gives a conclusion.

## 2. Adversary models

The adversary models we adopted are presented in [13], which is harsh but reasonable and widely accepted (see [48–51]). We also summarize the capabilities of the adversary  $\mathcal{A}$  in Table 1. We give a simple explanation of the capabilities.

As usual, the user's identity can be obtained in public channels, which always has a unified fixed format or chosen by the user randomly. Meanwhile, recently, Wang et al. [52,53] reveal that the password chosen by the user follows the Zipf's law. That means the space of passwords  $|D_{pw}|$  is extremely limited in practice. They usually assume that  $|D_{id}| \leq |D_{pw}| \leq 2^{20} \approx 10^6$ . Therefore, it is reasonable to set the capability C-01 that  $\mathcal{A}$  can enumerate the space of identity and password effectively in polynomial time.

Specially, we suppose the capability C-02 separately that  $\mathcal{A}$  can determine the victim  $U_i$ 's identity  $ID_i$ . A scheme is usually required to provide user anonymity, which means that  $\mathcal{A}$  neither knows which user this intercepted message comes from nor whether two messages are from the same user [54]. However, if  $\mathcal{A}$  desires to launch the impersonation attack, she can obtain the victim  $U_i$ 's identity  $ID_i$  by non-cryptographic methods (e.g., shoulder surfing). Thus, it is not contradictory for our supposed C-02 and the security goal of user anonymity.

Since the transmission of the message is in the insecure channel, C-1 is a common capability for  $\mathcal{A}$ . She can eavesdrop, intercept, insert, delete, and modify any transmitted messages over the public channel [55,56], which accords the Dolev–Yao model [10]. What is more, “Two-factor security” means that the users who have to know both two factors can be authenticated successfully. Therefore, the capability C-2 is usually used to analyze smart-card-based two-factor authentication protocols.

Last but not least, the capabilities C-3 and C-4 are presented to analyze the forward secrecy. It is common that  $\mathcal{A}$  can know the previous session key because of the insecure behaviors of insiders and users (e.g., delete incorrectly). What is more, when we evaluate the notion of forward secrecy, it is a convention that supposing  $\mathcal{A}$  can obtain the

**Table 2**  
Notations and abbreviations.

Symbol	Description
$U_i$	The $i$ th user
$S$	Cloud server
$\mathcal{A}$	Malicious attacker
$ID_i$	The identity of $U_i$
$PW_i$	The password of $U_i$
$x_s$	The private key of cloud server
$T_h$	The running time of hash function
$T_x$ or $\oplus$	The running time of bitwise XOR operation
$\oplus$	The XOR operation
$\otimes$	The NOR operation
$\parallel$	The concatenation operation
$h(\cdot)$	One-way hash function
$\rightarrow$	The public channel
$\Rightarrow$	The secure channel

server's long-time private keys [13,57,58]. The capabilities of adversary  $\mathcal{A}$  are indeed reasonable. Our analysis of three schemes will be based on these capabilities.

## 3. Cryptanalysis of Karupiah et al.'s scheme

Karupiah et al.'s [39] scheme is an enhancement over Kaul et al.'s scheme [40]. Karupiah et al. prove that their scheme is invulnerable to various attacks by using both rigorous formal and informal security proof. However, after our analysis, it is clear that the scheme cannot achieve its security goals.

### 3.1. Review of Karupiah et al.'s scheme

We will briefly review Karupiah et al.'s scheme [39]. This scheme consists of five phases: initialization, registration, log-in, authentication and password change. We simplify the initialization phase in the registration phase. For ease of description, some intuitive notations and abbreviates are listed in Table 2 and will be used through-out this paper.

#### 3.1.1. Registration phase

First, the parameters  $\{g, y, p\}$  are public parameters. And the cloud server has her own private key  $x_s$ . Then  $S$  gets public key  $y = g^{x_s} \pmod{p}$  using the generator  $g$ .

(1) User  $U_i$  freely selects identity  $ID_i$  and password  $PW_i$ . Then the user selects a random nonce  $k$  and uses  $k$  to compute  $HPW = h(PW_i \parallel k)$ .

(2)  $U_i \Rightarrow S : \{HPW, ID_i\}$ .

(3) Then the server  $S$  uses received message  $\{HPW, ID_i\}$  to compute  $A_i = h(ID_i \oplus x_s)$  and  $B_i = A_i \oplus h(ID_i \parallel HPW)$ . And the cloud server  $S$  uses a smart card  $SC$  to store parameters  $\{B_i, g, y, p, h(\cdot)\}$ .

(4)  $S \Rightarrow U_i : SC$ .

(5) After receiving the  $SC$ ,  $U_i$  computes  $N_i = k \oplus h(ID_i \oplus PW_i)$  and  $N_t = k \otimes ID_i \otimes PW_i$ . Then she stores  $\{N_i, N_t\}$  in the  $SC$ . Finally, the smart card contains  $\{B_i, g, y, p, h(\cdot), N_i, N_t\}$ .

#### 3.1.2. Log-in phase

(1) User  $U_i$  enters her  $ID_i$  and corresponding  $PW_i$ .

(2) Then smart card  $SC$  retrieves  $k = N_i \oplus h(ID_i \oplus PW_i)$  and use  $k$  to get  $N_i^* = k \otimes ID_i \otimes PW_i$ .

(3) After that, the  $SC$  gets  $A_i = B_i \oplus h(ID_i \parallel h(PW_i \parallel k))$  and  $W_i = h(T_u \oplus A_i) \oplus (r_i \oplus k)$  where  $r_i$  is a random number. Then the  $SC$  can also obtain  $C_i = g^{(r_i \oplus k)}$ ,  $DID = ID_i \oplus h(y^{(r_i \oplus k)})$ . And the smart card  $SC$  uses the present timestamp  $T_u$  to computes  $V_i = h(ID_i \parallel A_i \parallel W_i \parallel (r_i \oplus k) \parallel T_u)$ .

(4)  $SC \rightarrow S : \{C_i, W_i, V_i, DID, T_u\}$ .

### 3.1.3. Authentication phase

(1) After receiving the message,  $S$  uses her timestamp  $T_s$  to verify  $(T_s - T_u) \leq \Delta T$ . If  $T_u$  is invalid, then the  $S$  rejects the message.

(2) Then,  $S$  computes  $V_i^*$  and verifies  $V_i^* \stackrel{?}{=} V_i$ . If the verification is true,  $S$  authenticates  $U_i$ .  $S$  computes  $h(ID_i \parallel (A_i \oplus (r_i \oplus k))) = G_i$ . Then  $S$  uses  $G_i$  to get  $M_i = h(G_i \parallel T_s)$ .

(3)  $S \rightarrow U_i : \{M_i, T_s\}$ .

(4) Upon receiving the message  $\{M_i, T_s\}$ , time stamp  $T_s$  need to be verified.  $SC$  computes  $G_i^* = h(ID_i \parallel (A_i \oplus (r_i \oplus k)))$ . The  $SC$  uses  $G_i^*$  to compute  $M_i^* = h(G_i^* \parallel T_s)$ .  $SC$  verifies  $M_i^* \stackrel{?}{=} M_i$ . If it holds,  $U_i$  authenticates  $S$ .

(5) Next, the smart card and the server calculate  $SK_u = h(ID_i \parallel A_i \parallel (r_i \oplus k) \parallel (T_u \oplus T_s)) = SK_s$  separately for later communications.

### 3.1.4. Password change phase

(1) The  $ID_i$ ,  $PW_i$  and the new password  $PW_i^n$  are entered by  $U_i$  and then the user initiates a request to change the password.

(2)  $SC$  computes  $k = N_i \oplus h(ID_i \oplus PW_i)$  and  $HPW_i = h(k \parallel PW_i)$ . Then it computes  $N_i^* = k \otimes ID_i \otimes PW_i$ .

(3)  $SC$  checks whether  $N_i^* \stackrel{?}{=} N_i$ . If  $N_i^* \neq N_i$ ,  $SC$  ends the session; Otherwise, the smart card gets  $B_i^n = B_i \oplus h(ID_i \parallel h(PW_i \parallel k)) \oplus h(ID_i \parallel h(PW_i^n \parallel k)) = A_i \oplus h(ID_i \parallel HPW_i^n)$ . Then the  $SC$  computes  $N_i^n = N_i \oplus h(ID_i \oplus PW_i) \oplus h(ID_i \oplus PW_i^n) = k \oplus h(ID_i \oplus PW_i^n)$ ,  $N_i^n = k \otimes ID_i \otimes PW_i^n$ . Lastly,  $SC$  replaces  $\{B_i, N_i, N_i\}$  with  $\{B_i^n, N_i^n, N_i^n\}$ .

## 3.2. Cryptanalysis of Karupiah et al.'s scheme

Karupiah et al. [39] claim that their scheme can provide the session key (SK) security and resist the known attacks with lower computing and storage than other related schemes. However, we reveal that the scheme cannot achieve forward secrecy. What is more, it is also vulnerable to smart card loss attacks and insider attacks.

### 3.2.1. Smart card loss attack

Firstly, we suppose that  $\mathcal{A}$  can obtain  $U_i$ 's smart card and extract the parameters  $\{B_i, g, y, p, h(\cdot), N_i, N_i\}$  using side-channel attack [59,60]. What is more, the adversary can also intercept  $U_i$ 's log-in message  $\{C_i, W_i, V_i, DID, T_u\}$ , then she can obtain  $PW_i$  as follows:

**Step 1.**  $\mathcal{A}$  chooses  $ID_i^*, PW_i^*$  from  $D_{id} \times D_{pw}$ .

**Step 2.**  $\mathcal{A}$  computes  $k^* = N_i \oplus h(ID_i^* \oplus PW_i^*)$ .

**Step 3.**  $\mathcal{A}$  computes  $A_i^* = B_i \oplus h(ID_i^* \parallel HPW_i^*) = B_i \oplus h(ID_i^* \parallel h(PW_i^* \parallel k^*))$ .

**Step 4.**  $\mathcal{A}$  computes  $(r_i \oplus k)^* = W_i \oplus h(T_u \oplus A_i^*)$ .

**Step 5.**  $\mathcal{A}$  computes  $V_i^* = h(ID_i^* \parallel A_i^* \parallel W_i \parallel (r_i \oplus k)^* \parallel T_u)$ .

**Step 6.**  $\mathcal{A}$  check whether  $V_i^* = V_i$  to verify the correctness of  $(ID_i^*, PW_i^*)$  pair.

**Step 7.**  $\mathcal{A}$  repeats steps 1–6 until above equation holds, then the right values are found.

The time complexity of the attack procedure is  $\mathcal{O}((5T_h + 5T_{xor}) \times |D_{id}| \times |D_{pw}|)$ . It is clear that the time for  $\mathcal{A}$  to recover  $U_i$ 's password is a linear function of  $|D_{pw}| \times |D_{id}|$ . Nowadays, to meet user-friendliness, the users are allowed to choose  $ID$  and  $PW$  by themselves in most authentication schemes (e.g., [44,61]). Karupiah et al.'s scheme [39] also like the above principle. However, users usually choose the  $ID$  and  $PW$  which are low entropy and easy-to-remember. Since the password follows the Zipf's law [62] and the dictionary size is very restricted, usually  $|D_{id}| \leq |D_{pw}| \leq 2^{20} \approx 10^6$ . It is reasonable that  $\mathcal{A}$  can offline enumerate all the  $(ID, PW)$  pairs in polynomial time.

As it is known that the inherent cause of off-line password guessing attack is that  $\mathcal{A}$  can determine the correctness of the guess parameters by using a verifier. Specially, for the adversary  $\mathcal{A}$ , the verifier only contains one unknown parameter (i.e., password) which means all unknown parameters of the verifier can be derived from the password

and known parameters [63]. Ma et al. [30] proposed that the public-key techniques are necessary to resist off-line password guessing attack. It is obvious that the verifier is  $V_i$  in the above attack. Thus, we set  $R_1 = y^{r_1} \bmod p$ ,  $R_0 = g^{r_1} \bmod p$ , where  $y$  is server's public key and  $r_1$  is a random number. We reset  $V_i = h(ID_i \parallel A_i \parallel W_i \parallel (r_i \oplus k) \parallel T_u \parallel R_1)$ . Then the user sends message  $\{C_i, W_i, V_i, DID, T_u, R_0\}$  to the server. When the server receives the message, she uses her secret key  $x_s$  to calculate  $R_1^* = R_0^{x_s} = g^{r_1 x_s} \bmod p$ . Then the server gets other parameters as the original scheme. She can authenticate user's identity by calculating  $V_i^* = h(ID_i \parallel A_i \parallel W_i \parallel (r_i \oplus k) \parallel T_u \parallel g^{r_1 x_s})$ .

What is more, after the server authenticates use's identity, she will calculate  $G_i, M_i$ . The  $M_i$  in original Karupiah et al.'s scheme [39] can also be used to apply off-line password guessing attacks. The attack steps are similar to the above attack. Therefore, we also reset  $G_i = h(ID_i \parallel (A_i \oplus (r_i \oplus k)) \parallel R_2)$  and  $M_i = h(G_i \parallel T_s)$ , where  $r_2$  is a random number and  $R_2 = g^{r_2} \bmod p$ . Then the server gets  $R_3 = g^{r_2} \bmod p$  and sends  $\{M_i, T_s, R_3\}$  to the user. Then the  $SC$  computes  $G_i^* = h(ID_i \parallel (A_i \oplus (r_i \oplus k)) \parallel R_3^1)$ ,  $M_i^* = h(G_i^* \parallel T_s)$ . The  $SC$  ensures server's identity by verifying  $M_i^* \stackrel{?}{=} M_i$ .

After that, if the adversary  $\mathcal{A}$  desire to use off-line guessing attack to candidate user's password. She needs to get a verifier to confirm the correctness of the password [63]. However, the attacker cannot use  $(ID, PW)$  she guessed to represent  $V_i$  or  $M_i$ . The adversary cannot obtain  $r_1, r_2$  by  $R_0, R_3$  because it is a computational Diffie-Hellman problem [64] which cannot be solved in polynomial time. Consequently, our improvement measure is available and secure.

### 3.2.2. Insider attack

Suppose  $\mathcal{A}$  is a malicious server administrator.  $\mathcal{A}$  can intercept  $U_i$ 's registration message  $\{ID_i, HPW\}$ , and she can also stole or pick up  $U_i$ 's smart card and extract  $\{B_i, g, y, p, h(\cdot), N_i, N_i\}$ . The malicious administrator can compute  $U_i$ 's password by the following steps:

**Step 1.**  $\mathcal{A}$  chooses  $PW_i^*$  from  $D_{pw}$ .

**Step 2.**  $\mathcal{A}$  computes  $k^* = N_i \oplus h(ID_i \oplus PW_i^*)$ .

**Step 3.**  $\mathcal{A}$  computes  $HPW^* = h(PW_i^* \parallel k^*)$ .

**Step 4.**  $\mathcal{A}$  verifies whether  $HPW^* = HPW$ .

**Step 5.**  $\mathcal{A}$  repeats the steps 1 ~ 4 until above equation holds.

In fact, many websites and applications are attacked because of malicious server administrators, which causes the disclosure of user personal information. Therefore, we can reasonably assume that attackers can intercept or internally extract  $U_i$ 's registration information. The time complexity of this attack is  $\mathcal{O}((2T_h + 2T_{xor}) \times |D_{pw}|)$ . The attacker can achieve this attack in polynomial time.

In this scheme, the verifier  $HPW$  contains two parameters  $PW_i$  and  $k$ . Unfortunately,  $k$  can be computed using the parameters  $N_i$ . A possible countermeasure to resist this attack is that the user updates  $k$  after registration. When the server  $S$  sends smart card to the  $U_i$ , the  $U_i$  can select a new nonce  $k'$ . Then updating  $HPW' = h(PW_i \parallel k')$  and  $B_i = A_i \oplus h(ID_i \parallel HPW')$ . What is more,  $N_i = k' \oplus h(ID_i \oplus PW_i)$  and  $N_i = k' \otimes ID_i \otimes PW_i$ . Then the user stores  $\{N_i, N_i\}$  in the  $SC$ .

When we adapt this countermeasure, the malicious administrator cannot launch above attack. The malicious insider could get  $N_i$  and  $HPW$  as mentioned before. If she desires to verify the correctness of  $PW_i$ , she needs to get a parameter  $k$ . And then she calculates  $HPW^* = h(PW_i^* \parallel k^*)$ . However, in our countermeasure, we update new parameter  $k'$  to calculate  $N_i$  after the user's registration. Therefore, the adversary cannot get parameters  $k$  by using the  $PW_i$  she guessed. The attacker cannot get the user's password or other related parameters, so our countermeasure can resist insider attack.

**Table 3**  
Notations and abbreviations.

Symbol	Description
$SA$	The system authority
$UID_i$	The username of $i$ th user
$ST$	The security token
$x_s$	The private key of cloud server
$Y_s$	The public key of cloud server
$K_{sa}$	The master key of system authority
$T_m^e$	The running time of modular exponentiation
$H(\cdot)$	One-way hash function
$F(\cdot)$	One-way hash function
$E(\cdot)/D(\cdot)$	Symmetric encryption/decryption function

### 3.2.3. No forward secrecy

We claim that  $\mathcal{A}$  has the capabilities C-02 and C-4. When analyzing the forward security of the protocol, we suppose that  $\mathcal{A}$  knows  $S$ 's long-time secret key  $x_s$ . And  $\mathcal{A}$  can obtain the messages  $\{C_i, W_i, V_i, DID, T_u\}$  and  $\{M_i, T_s\}$ . According to the following steps,  $\mathcal{A}$  can get the session key.

**Step 1.**  $\mathcal{A}$  computes  $A_i = h(ID_i, x_s)$ .

**Step 2.**  $\mathcal{A}$  computes  $(r_i \oplus k) = W_i \oplus h(T_u \oplus A_i)$ .

**Step 3.**  $\mathcal{A}$  computes

$$SK = h(ID_i \parallel A_i \parallel (r_i \oplus k) \parallel (T_u \oplus T_s)).$$

The time complexity of this attack is  $\mathcal{O}(3T_h + 3T_{xor}) \times |D_{pw}|$ . Moreover, in the above attack, we suppose that  $U_i$ 's  $ID_i$  can be known by some non-cryptographic methods, because the user's  $ID_i$  is regarded as a kind of public information on some websites (e.g., telephone number, social security account). Thus, it is reasonable that  $\mathcal{A}$  can calculate the session key in polynomial time. In a word, Karuppiah et al.'s scheme [39] cannot attain forward secrecy.

Following Ma et al.'s principle [30], to resist this attack, the public key technique and two modular exponentiations are required on the server side. We can set  $R_1 = y^{r_1} \bmod p$  and  $R_0 = g^{r_1} \bmod p$ , where  $r_1$  is randomly selected by the user. Then the user replaces message  $\{C_i, W_i, V_i, DID, T_u\}$  by message  $\{C_i, W_i, V_i, DID, T_u, R_0\}$  and sends to server. The server computes  $R_2 = g^{r_2 r_1} \bmod p$  and  $R_3 = g^{r_2} \bmod p$ , where  $r_2$  is a random number. She sends  $\{M_i, T_s, R_3\}$  to the user. Lastly, the users computes  $SK_u = h(ID_i \parallel A_i \parallel (r_i \oplus k) \parallel (T_u \oplus T_s) \parallel R_3^{r_1})$ . And the server computes  $SK_s = h(ID_i \parallel A_i \parallel (r_i \oplus k) \parallel (T_u \oplus T_s) \parallel R_2)$ . As such, the adversary cannot compute  $r_1$  or  $r_2$  within polynomial time (it is a computational Diffie–Hellman problem). Then the attacker cannot get the session key. Therefore, our method is useful to protect the scheme's forward secrecy.

## 4. Cryptanalysis of Lin's scheme

Lin [37] proposes an anonymous two-factor authentication scheme. Lin claims that his scheme allows a user to choose a pseudo-identity for remote authentication in cloud environments. What is more, he claims the scheme can achieve user anonymity. Although the scheme is different from traditional schemes, we also find it is vulnerable to smart card loss attack and cannot achieve forward secrecy.

### 4.1. Review of Lin's scheme

We briefly review Lin's [37] scheme, which involves four phases: setup, user registration, authentication and password update. We simplify the setup phase in the registration phase. the intuitive abbreviations are listed in Table 2 and some additional ones in Table 3. In this scheme, some used notations are different. The username  $UID_i$  is randomly selected by the user (e.g., a nickname) and  $ID_i$  is a fixed format number used to represent the user's identity.

#### 4.1.1. Registration phase

Initially, the system authority  $SA$  owns a master secret key  $K_{sa}$ . She first generates  $p, q$  and a generator  $g$  of order  $q$ . The client  $U_i$ 's identity is  $ID_i$ , which is usually a fixed parameter assigned by the system.  $U_i$  has her own username  $UID_i$  and corresponding password  $PW_i$ . Then the user  $U_i$  will register to  $S$  through the system authority  $SA$ .

(1)  $U_i$  computes  $e_i = H(PW_i \oplus r_i, UID_i, ID_{cs})$  and  $\delta_i = H(PW_i \oplus r_i, UID_i, ID_i)$ , where  $r_i$  is a nonce selected from  $Z_p$ .

(2)  $U_i \Rightarrow SA : \{ID_i, e_i\}$ .

(3) If  $ID_i$  has not registered before, the SA generates a pseudo-identity for  $ID_i$  as  $PID_i = E_{K_{sa}}(ID_i \oplus Y_{cs})$ .

(4)  $SA \Rightarrow S : \{PID_i, e_i\}$ .

(5) Then  $S$  computes  $k_i = F(PID_i, x_s)$ ,  $\sigma_i = k_i \parallel Y_s$ ,  $\tau_i = \sigma_i \oplus e_i$ ,  $\eta_i = PID_i \oplus e_i \oplus H(x_s)$ , and stores  $(\eta_i, Y_s, \tau_i)$  in a security token hardware  $ST_i$ .

(6)  $S \Rightarrow U_i : ST_i$ .

(7) Finally,  $U_i$  further stores  $(r_i, \delta_i)$  into  $ST_i$ .

#### 4.1.2. Authentication phase

(1)  $U_i$  first enters  $UID_i$  and  $PW_i$  to the security token  $ST_i$ , then  $ST_i$  calculates  $e_i = H(PW_i \oplus r_i, UID_i, ID_{cs})$ ,  $\sigma_i = \tau_i \oplus e_i = k_i \parallel Y_s'$ , and checks if  $Y_s' = Y_s$ . Otherwise, it aborts.

(2) Next,  $ST_i$  chooses a random number  $a \in_R Z_q$ . Then  $ST_i$  uses  $a$  to compute  $\beta = (Y_{cs}')^a \bmod p$ ,  $CID_i = \eta_i \oplus e_i$ ,  $c_1 = \beta \oplus CID_i$ ,  $c_0 = g^a \bmod p$ ,  $d_i = H(CID_i, c_0, \beta, T_1)$ , and  $c_2 = d_i \oplus k_i$ .

(3)  $U_i \rightarrow S : \{c_0, c_1, c_2, T_1\}$ .

(4)  $S$  first checks whether  $T_1$  is fresh or valid.  $S$  further computes  $\beta' = c_0^{x_s} \bmod p$ ,  $CID_i' = \beta' \oplus c_1$ ,  $d_i' = H(CID_i', c_0, \beta', T_1)$ ,  $k_i' = F(CID_i', x_s)$ ,  $c_2' = d_i' \oplus k_i'$  and verifies if  $c_2' = c_2$ ; Else,  $S$  denies the log-in request. Then,  $S$  chooses  $b \in_R Z_q$  to compute  $VK = H(d_i', k_i' \oplus b, ID_{cs})$ ,  $c_3 = VK \oplus \beta'$ .

(5)  $S \rightarrow U_i : \{c_3, b\}$ .

(6)  $U_i$  derives  $VK' = H(d_i, k_i \oplus b, ID_{cs})$  and verifies the equation of  $c_3 = VK' \oplus \beta$ .

#### 4.1.3. Password-update

The user  $U_i$  first enters  $ID_i, UID_i$  along with passwords  $(PW_i, PW_i')$  to the security token  $ST_i$ . After that,  $ST_i$  computes  $e_i' = H(PW_i' \oplus r_i, UID_i, ID_{cs})$ ,  $e_i^* = H(PW_i' \oplus r_i, UID_i, ID_{cs})$ , and  $\delta_i^* = H(PW_i' \oplus r_i, UID_i, ID_i)$ . Then  $ST_i$  checks whether  $\delta_i^* = \delta_i$ ; Next,  $ST_i$  can update the stored  $(\tau_i, \delta_i)$  as  $\tau_i' = \tau_i \oplus e_i \oplus e_i^*$ ,  $\delta_i' = H(PW_i' \oplus r_i, UID_i, ID_i)$ .

## 4.2. Cryptanalysis of Lin's scheme

Lin [37] shows that the proposed scheme is invulnerable to various attacks together with attacks observed in the analyzed scheme and proves the security of the proposed scheme in the random oracle model. However, we use reasonable and widely accepted adversary models to analyze this scheme and find that it cannot resist smart card loss attacks and cannot achieve forward secrecy.

### 4.2.1. Smart card loss attack

Suppose  $\mathcal{A}$  has obtained user  $U_i$ 's security token hardware  $ST_i$  and uses side-channel attacks to extract  $(\eta_i, Y_s, \tau_i, r_i, \delta_i)$ . Then she can obtain  $PW_i$  following the steps blow:

**Step 1.**  $\mathcal{A}$  chooses  $UID_i^*, PW_i^*$  from  $D_{uid} \times D_{pw}$ .

**Step 2.**  $\mathcal{A}$  computes  $\delta_i^* = H(PW_i^* \oplus r_i, UID_i^*, ID_i)$ .

**Step 3.**  $\mathcal{A}$  verifies whether  $\delta_i^* = \delta_i$ .

**Step 4.**  $\mathcal{A}$  repeats step 1–3 until equation holds.

In this scheme, user's  $ID_i$  is a fixed number represented user's identity (e.g., ID Card number). As usual, we assume that  $ID_i$  is a known parameter because  $\mathcal{A}$  can get user's identity through public channels, such as hacker websites, etc. The time complexity of this attack is  $\mathcal{O}(|D_{uid}| \times |D_{pw}| \times (T_h + T_{xor}))$ . Therefore,  $\mathcal{A}$  can lunch above attack in polynomial time.

The possible countermeasure is that we reset  $\delta_i = H(PW_i \oplus r_i, UID_i, ID_i) \pmod{n_0}$ , where  $n_0$  is an integer and  $n_0 \in (2^4, 2^8)$ . After that,  $\mathcal{A}$  can candidate  $|D_{uid} \times D_{pw}|/n_0 \approx 2^{32}$  pairs of  $(UID_i, PW_i)$ , which satisfy the equation  $\delta_i = \delta_i^*$ . However, only one pair of  $(UID_i, PW_i)$  is correct. In order to get the correct one, the adversary has to initiate the log-in request to the server, which will be detected and rejected by the server. Because the number of incorrect user identity and password is limited (generally 5–10 times). Thus,  $\mathcal{A}$  usually cannot get the correct  $(UID_i, PW_i)$  from  $2^{32}$  pairs of  $(UID_i, PW_i)$  within 10 times, so she cannot launch smart loss attacks in this scheme.

#### 4.2.2. No forward secrecy

Suppose  $\mathcal{A}$  can obtain the cloud server  $ID_{cs}$ 's long-time secret key  $x_s$ . She also intercepts user log-in message  $\{c_0, c_1, c_2, T_1\}$  and server response  $\{c_3, b\}$ . Then she can obtain previous session key  $VK$  as follows:

**Step 1.**  $\mathcal{A}$  computes  $\beta' = c_0^{x_s} \pmod{p}$ .

**Step 2.**  $\mathcal{A}$  computes  $VK = c_3 \oplus \beta'$ .

Suppose  $\mathcal{A}$  obtains previous session key  $VK_j$ , then she can compute the  $j$ th session key  $VK_j$ .

**Step 1.**  $\mathcal{A}$  computes  $\beta_i = c_{3i} \oplus VK_j$ .

**Step 2.**  $\mathcal{A}$  computes  $CID_j = CID_j \oplus \beta_i$ .

**Step 3.**  $\mathcal{A}$  computes  $\beta_j = CID_j \oplus c_{1j}$ .

**Step 41.**  $\mathcal{A}$  computes  $VK_j = \beta_j \oplus c_{3j}$ .

The time complexity of attack  $\infty$  is  $\mathcal{O}(T_{me} + T_{xor})$ . And the time complexity of attack 2 is  $\mathcal{O}(4T_{xor})$ . Despite Lin's scheme [37] has paid attention to forward secrecy issue, it still violates the "PFS principle" suggested in Ma et al. [30]. There is only one exponentiation operation on the server side. Accordingly, similar to Section 3.2.3, we assume  $r_1, r_2$  are two random numbers selected separately by the server and the user. The user computes  $c_4 = g^{r_1} \pmod{p}$  and the server gets  $c_5 = g^{r_2} \pmod{p}$ . Then they send  $c_4, c_5$  to each other. The session key  $VK$  can be recalculated as  $VK' = H(d_i, k_i \oplus b, ID_{cs}, g^{r_1 r_2})$ . After slight modification, Lin's scheme [37] can provide forward secrecy and resist above attack successfully.

## 5. Cryptanalysis of Rajamanickam et al.'s scheme

In 2020, Rajamanickam et al. [38] propose a lightweight password-based single-factor authentication scheme for Internet applications, which claimed to resist insider attacks and other security issues. However, we reveal that their scheme is not actually resistant to insider attacks. What is more, it also cannot achieve forward secrecy and user anonymity.

### 5.1. Review of Rajamanickam et al.'s scheme

We will describe Rajamanickam's scheme proposed in 2020 [38], which claims to resist insider attack and achieve their claimed security goals. The scheme includes three main phases: initial setup, registration, log-in and authentication. For ease of description, some intuitive notations and abbreviations are listed in Tables 4 and 2.

#### 5.1.1. Initial setup

SPS first sends its identity  $ID_{SPS}$  to the PMS through an insecure channel. Then PMS generates a master secret key  $MSK_j$ , gets public key  $P_{pub} = MSK_j \cdot P$  and sends  $MSK_j$  to the SPS in a secure channel. Then PMS stores  $(ID_{SPS}, MSK_j)$  in a table encrypted by PMS's secret key  $s_{PMS}$ . And the corresponding public key of PMS's secret key is  $pub_{PMS} = s_{PMS} \cdot P$ .

**Table 4**

Notations and abbreviations.

Symbol	Description
$SPS$	Service provider server
$PMS$	Password management server
$ID_{SPS}$	The identity of $SPS$
$MSK_j, P_{pub}$	Master secret key, public key of $SPS$
$pub_{PMS}, s_{PMS}$	Public key, secret key of $PMS$
$T_{mul}$	The running time of ECC multiplication
$T_{dec}$	The running time of decryption in ECC
$E(\cdot)$	ECC encryption
$AES(\cdot)$	AES encryption

#### 5.1.2. Registration phase

When the client  $U_i$  desires to enjoy the services of the SPS, she need to register first. (1)  $U_i$  chooses the username  $ID_i$  and the password  $PW_i$ . Then she enters  $(ID_i, PW_i)$  to the web browser. The browser gets  $E_{pub_{PMS}}(ID_i, PW_i)$  by using PMS's public key  $pub_{PMS}$ .

(2)  $U_i \rightarrow PMS: E_{pub_{PMS}}(ID_i, PW_i)$ .

(3) When receiving the message, the PMS decrypts and computes  $A_i = h((h(ID_i) \oplus h(PW_i)) \pmod{n})$  and  $B_i = h((h(ID_{SPS}) \oplus h(A_i)) \pmod{n})$ . Then she encrypts  $A_i$  and  $B_i$  by  $MSK_j$  to make ciphertext  $C_i = AES_{MSK_j}(A_i, B_i, TID_i)$ , where  $TID_i = h(ID_i)$ . The PMS maintains different tables for different SPSs. Every table stores data  $TID_i = h(ID_i)$ ,  $A_i$  and  $E_{s_{PMS}}(PW_i)$ .

(4)  $PMS \rightarrow SPS: \{C_i, n\}$ .

(5)  $PMS \rightarrow U_i: \text{a confirmation message}$ .

(6) The SPS decrypts message to get  $A_i, B_i$  and  $TID_i$ . She computes  $B_i^* = h((h(ID_{SPS}) \oplus h(A_i)) \pmod{n})$ . After that, SPS checks  $B_i^* \stackrel{?}{=} B_i$ . If it do not holds, the SPS will end the conversation. Otherwise, the SPS stores  $TID_i$  and  $A_i$  in a secure manner.

#### 5.1.3. Log and authentication phase

(1)  $U_i$  first provides  $ID_i$  and  $PW_i$  to the web browser. Then the browser gets  $A_i^* = h((h(ID_i) \oplus h(PW_i)) \pmod{n})$ ,  $TID_i^* = h(ID_i)$ . After that, the web browser chooses the nonce  $r_1$  and computes  $D_1 = r_1 \cdot P$ ,  $E_i = h(ID_{SPS} \parallel D_1 \parallel A_i \parallel T_1)$ , where  $T_1$  is a timestamp. Moreover,  $U_i$  encrypts  $TID_i^*$  by SPS's public key  $P_{pub}$  and computes  $F_i = E_{P_{pub}}(TID_i^*)$ ,  $G_i = TID_i^* \oplus r_1$ .

(2)  $U_i \rightarrow SPS: \{E_i, F_i, G_i\}$ .

(3) The SPS verifies  $|T_1 - T_2| \leq \Delta T$  firstly. If it holds, the SPS computes  $TID_i^*$  by using  $MSK_j$ . Then the SPS searches the table and obtains  $A_i$ . Then the SPS computes  $r_1^* = G_i \oplus TID_i^*$ ,  $D_1^* = r_1^* \cdot P$ ,  $E_i^* = h(ID_{SPS} \parallel D_1^* \parallel A_i \parallel T_1)$ , and checks whether  $E_i^* \stackrel{?}{=} E_i$ . If it holds, the SPS chooses a nonce  $r_2$ . Then SPS gets  $R_i = r_1 \oplus r_2$ ,  $CK = r_2 \cdot D_1^*$  and  $K_i = h(ID_{SPS} \parallel CK \parallel A_i \parallel T_2)$ .

(4)  $SPS \rightarrow U_i: \{K_i, R_i, T_2\}$ .

(5) The user  $U_i$  first checks the timestamp, then  $U_i$  get  $r_2^* = R_i \oplus r_1$  and computes  $CK^* = r_2^* \cdot D_1$ ,  $K_i^* = h(ID_{SPS} \parallel CK^* \parallel A_i \parallel T_2)$ . After that,  $U_i$  checks whether  $K_i^* = K_i$ . Then, the session key of the client  $U_i$  and the SPS is  $CK = CK^* = r_1 \cdot r_2^* \cdot P$ .

### 5.2. Cryptanalysis of Rajamanickam et al.'s scheme

Rajamanickam et al. [38] claim that their scheme can resist insider attacks. However, after our analysis, we reveal that the scheme proposed by Rajamanickam et al. [38] cannot resist insider attacks. And it can neither provide forward secrecy nor user anonymity.

#### 5.2.1. Insider attack

According to the capabilities of the attacker in Section 2, suppose  $\mathcal{A}$  is a malicious SPS administrator, she can obtain the message  $\{A_i, TID_i\}$  stored in SPS. And  $\mathcal{A}$  can also intercept  $\{C_i, n\}$  and perform offline password guess. We show this attack as follows:

**Step 1.**  $\mathcal{A}$  chooses a pair  $(ID_i^*, PW_i^*)$  from  $D_{id} \times D_{pw}$ .

- Step 2.**  $\mathcal{A}$  computes  $A_i^* = h((h(ID_i^*) \oplus h(PW_i^*)) \bmod n)$ .
- Step 3.**  $\mathcal{A}$  verifies the correctness of  $(ID_i^*, PW_i^*)$  by checking whether  $A_i^* = A_i$ .
- Step 4.**  $\mathcal{A}$  repeats the steps 1 ~ 3 until the correct values are found.

In this scheme, they attempt to provide off-line password guess attack resistance by employing “fuzzy-verifier” technique [13]. However, we find they use the wrong “fuzzy verifier”. It is invalid and even makes the situation worse. Specifically, in the above attack,  $\mathcal{A}$  can find  $(|D_{id}| \times |D_{pw}|)/n$  pair of  $(ID_i^*, PW_i^*)$  satisfied equation  $A_i = h((h(ID_i^*) \oplus h(PW_i^*)) \bmod n)$ . As it is known that, if the  $\mathcal{A}$  desire to pass the authentication from the server, she has to know the legitimate user’s  $ID$  and  $PW$ . Unfortunately,  $A_i$  is the key parameter to help the server authenticate user, which means  $\mathcal{A}$  can use  $(|D_{id}| \times |D_{pw}|)/n$  pair of  $(ID_i^*, PW_i^*)$  to impersonate user pass the authentication of the server. In a word, their method does not only increase the difficulty of attack, but also make the attack easier. The time complexity of the attacking procedure is  $\mathcal{O}((|D_{id}| \times |D_{pw}|)/n) \times (3T_h + T_{xor} + T_{mod})$ .

In their scheme, there is no verifier in the log-in phase. That means their scheme cannot provide a mechanism to check the validity of passwords in real time and detect the malicious attackers. We propose a possible countermeasure that using Wang et al. [13]’s “fuzzy-verifier” technique to solve this flaw. Firstly, the web browser computes  $V_i = h(h(ID_i) \oplus h(PW_i \parallel a) \bmod n)$ . Then the browser stores it in a table. After that, if the user desires to log-in, she needs to enter her  $ID_i^*, PW_i^*$ . Then the web browser computes  $V_i^*$  and checks whether  $V_i^* \stackrel{?}{=} V_i$ . Last but not least, the web browser provides timely detection mechanism for mistyped pair of  $(ID_i, PW_i)$ , which will resist off-line password guessing attacks.

### 5.2.2. No forward secrecy

Unfortunately, Rajamanickam et al.’s [38] scheme cannot provide forward security. In case the SPS’s master secret key  $MSK_j$  has been compromised by an adversary  $\mathcal{A}$ .  $\mathcal{A}$  can intercept the messages  $\{E_i, F_i, G_i\}$  and  $\{K_i, R_i, T_2\}$ . With the extracted  $MSK_j$  and message,  $\mathcal{A}$  can obtain the session key. We show the steps as follows:

- Step 1.**  $\mathcal{A}$  extracts  $TID_i^*$  from  $F_i$  using the master secret key  $MSK_j$ .
- Step 2.**  $\mathcal{A}$  computes  $r_1 = G_i \oplus TID_i^*$ .
- Step 3.**  $\mathcal{A}$  computes  $r_2 = R_i \oplus r_1$ .
- Step 4.**  $\mathcal{A}$  computes  $CK = r_1 \cdot r_2 \cdot P$ .

The time complexity of the attack is  $\mathcal{O}(T_{ecc} + 2T_{xor} + 2T_{mul})$ . The result means that the above attack is quite efficient. Generally speaking, to achieve forward secrecy, the SK usually consists of two fresh random numbers which cannot be obtained in the open channel. However, in the above attack,  $\mathcal{A}$  can obtain two random numbers  $r_1$  and  $r_2$ . There is not simple solution to resist this attack, which means the designers need to redesign the scheme fundamentally.

### 5.2.3. No user anonymity

In this scheme, Rajamanickam et al. [38] claim that the proposed  $U_i$ ’s  $ID$  is never disclosed to the SPS. However, with our analysis, this protocol cannot achieve this goal. The user’s identity can be extracted by the following steps. Suppose  $\mathcal{A}$  is a server administrator.

- Step 1.**  $\mathcal{A}$  chooses a  $ID_i^*$  from  $D_{id}$ , where  $D_{id}$  represents the identity space.
- Step 2.**  $\mathcal{A}$  extracts  $TID_i$  from server.
- Step 3.**  $\mathcal{A}$  computes  $TID_i^* = h(ID_i^*)$ .
- Step 4.**  $\mathcal{A}$  check if  $TID_i^* = TID_i$ . If not,  $\mathcal{A}$  repeat step 1–3 until find correct  $ID_i$ .

The time complexity of above attack is  $\mathcal{O}(|D_{id}| \times T_h)$ . The above attack can be effectively implemented in polynomial time, thus,  $\mathcal{A}$  can exploit the user’s identity, which means that this scheme cannot realize their claimed goal.

## 6. Some lessons learned

It has proved that despite decades of development, designing a secure password-based authentication scheme is still hard work. Most protocol designers only think about the modification and enhancement of a single protocol, but few people consider the general design principles of a certain type of protocol. In 2014, Ma et al. [30] proposed three vital design principles for secure two-factor schemes based on smart cards, which has made a profound impact on the development of designing a secure scheme.

### (1) The public key principle

In 1999, Halevi-Krawczyk [56] proposed a principle that password-based single-factor authentication scheme cannot resist off-line guess attack by only using symmetric cryptographic primitives. Based on this principle, Ma et al. [30] proposed and proved that two-factor authentication scheme based on smart card cannot resist off-line password guessing attacks if they do not employ public-key techniques. Moreover, when we consider n-factor security, we usually suppose that adversary can get  $n - 1$  factors which means n-factor security schemes will become a traditional two-factor security scheme. Therefore, Ma et al.’s principle [30] is also suitable for multi-factor authentication.

### (2) The security-usability trade-off principle

The smart card storing a verifier to achieve “local password update” will lead to off-line password guessing attacks. That means when the designers have to make trade-offs when they choose to provide the function of “local password update” or achieve the property of “resistance against off-line password guess attack” in their schemes.

### (3) The forward secrecy principle

When we analyze the forward secrecy, we usually suppose the adversary can eavesdrop server’s long-term secret key. Ma et al. [30] proposed that forward secrecy cannot be achieved without the public-key technique in the schemes and the server should conduct at least two exponential operations or point multiplication.

Though these three principles are proposed for two-factor schemes, it is also suitable for password-based multi-factor authentication schemes. Furthermore, they are also used in various environments such as cloud services, industrial IoT, WSN. Besides, there are still other principles of protocol design (e.g., [13,54,67]). Accordingly, we find that the reason why the three schemes [37–39] are vulnerable to various attacks is that they do not consider the protocol design principles. We have analyzed that the three schemes mentioned above are vulnerable to various attacks and cannot achieve security goals. To learn some lessons, we summarize the flaws of the three schemes and discuss the principles they violated in Table 5. For instance, the smart card attack in Section 4.2.1 is mainly due to violating Ma et al.’s “security-usability” trade-off principle [30] and it also does not use the “fuzzy-verifier” technique [13] to solve this situation. What is more, the vulnerabilities reported in Sections 3.2.3, 4.2.2 and 5.2.2 are mainly due to the violation of Ma et al.’s “forward secrecy principle” [30]. It also reflects the importance of meeting the requirements of the three basic principles for designing a secure protocol. Therefore, we also reveal a series of two-factor or multi-factor schemes proposed recently [37–47] and show in Table 6 that most of them are mostly typical invalid protocols which do not respect the three principles mentioned above and cannot achieve indeed security.

## 7. Conclusion

In this work, we analyze three different authentication schemes for cloud environments presented by Karupiah et al. [39], Lin [37] and Rajamanickam et al. [38], which are designed for cloud environments. We demonstrate that they all suffer from security attacks (e.g., smart card loss attack, insider attack) and fail to achieve forward secrecy. In order to draw some lessons, we summarize the causes of these flaws and propose possible countermeasures (e.g., “fuzzy-verifier”, update parameter after login) to overcome these pitfalls. Meanwhile, we reveal

**Table 5**  
Summary of our cryptanalysis results and the underlying vulnerabilities.

Scheme	Weakness	Vulnerabilities exploited
Karupiah et al. [39]	Smart card loss attack (See Section 3.2.1)	The user does not correctly use public key cryptography to construct the log-in message [30].
	Insider attack (See Section 3.2.2)	When the attacker obtains user's smart card, the security of user's password is affected [65,66].
	No forward secrecy (See Section 3.2.3)	At least two exponentiations are needed at the server side to achieve forward security [30].
Lin [37]	Smart card loss attack (See Section 4.2.1)	The smart card stores an explicit password verification verifier which violates the "security-usability trade-off principle" in [9,30].
	No forward secrecy (See Section 4.2.2)	At least two exponentiations are needed at the serverside to achieve forward security [30].
Rajamanickam et al. [38]	Smart card loss attack (See Section 5.2.1)	The authentication server should not store sensitive parameters of the user to avoid insider attacks [30].
	No forward secrecy (See Section 5.2.2)	At least two exponentiations are needed at the serverside to achieve forward security [30].

**Table 6**  
A summary of the violation of three protocol design principles in recent schemes.

Principle	Kaul et al. [40]	Karupiah et al. [39]	Lin [37]	Rajamanickam et al. [38]	Roy et al. [41]	Guo et al. [42]	Ostad-Sharif et al. [43]	Kaura et al. [44]	Gope et al. [45]	Chaudhry et al. [46]	Ayub et al. [47]
Public key principle [30]	✓	✓	✓	✓	×	×	×	✓	×	✓	✓
Security-usability trade-off principle [30]	✓	×	✓	✓	×	×	×	✓	×	×	×
Forward secrecy principle [30]	×	×	×	×	×	×	×	×	×	✓	✓

Note that "✓" means achieving the corresponding principle, while "×" not.

that it is necessary for protocol designers to follow the three principles of protocol design (i.e. the public key principle, the security-usability trade-off principle and the forward secrecy principle) proposed by Ma et al. [30]. We also analyzed whether a dozen recently proposed schemes follow the above three principles. After our analysis, there are still many protocol designers who do not pay attention to the importance of the principle of designing protocol, which leads to attacks on the protocol. How to design a truly two-factor secure authentication scheme under the protocol design principles is still a huge challenge. In the future work, we will pay more attention to this.

**Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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**Meijia Xu** received the B.S. degree in information security from the China University of Mining and Technology, P. R. China, in Jun. 2020. She is currently working toward the M.S. degree from the College of Cyber Science, Nankai University, Tianjin, P. R. China. Her research interests include applied cryptography and password-based authentication.



**Ding Wang** received his Ph.D. degree in Information Security at Peking University in 2017. He is currently a Professor at College of Cyber Science, Nankai University, and also serves as the deputy director of the Tianjin key laboratory of Network and Data Security Technology. As the first author or corresponding author, he has published more than 60 papers at venues like ACM CCS, Usenix Security, NDSS, IEEE DSN, ESORICS, ACM TCPS, IEEE TDSC and IEEE TIFS. Six of them are recognized as “ESI highly cited papers”. His Ph.D. thesis receives the “ACM China Doctoral Dissertation Award” and “China Computer Federation (CCF) Outstanding Doctoral Dissertation Award”. He has been involved in the community as a TPC member, AEC member or PC Chair for over 50 international conferences such as Usenix Security, PETS, ACSAC, ASIACCS, SEC, ISC and ACISP. His research interests include password, multi-factor authentication and provable security.



**Qingxuan Wang** received the M.S. degree in information security from the China University of Geosciences, Wuhan, P. R. China, in Jun. 2020. He is currently working toward the Ph.D. degree from the College of Cyberspace Security, Nankai University, Tianjin, P.R. China. His research interests include applied cryptography and password-based authentication.



**Qiaowen Jia** is currently a Ph.D. candidate in Institute of Software, University of Chinese Academy of Sciences. Her research interest includes concurrent program and software verification.